

Digital Knowledge: From Facts to Rules and Back

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03.05.2017

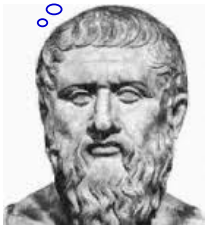
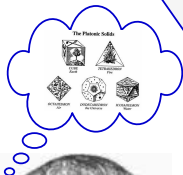


What is Knowledge?

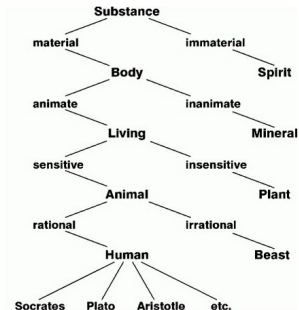
Plato: *“Knowledge is justified true belief”*

Personal

350 BC



External



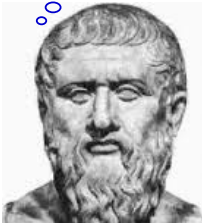
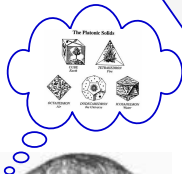
Tree of Knowledge

What is Knowledge?

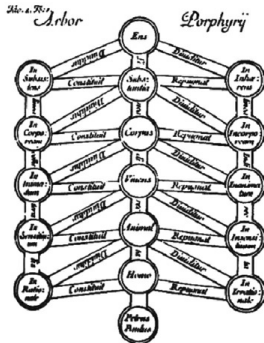
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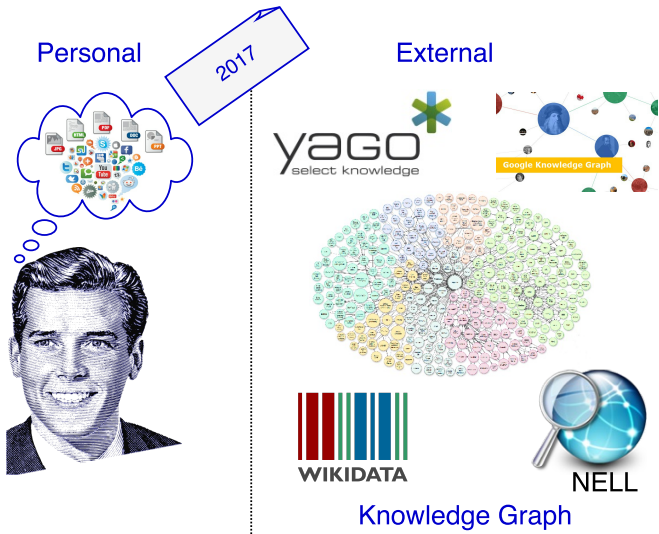


External



What is Digital Knowledge?

“Digital knowledge is semantically enriched machine processable data”



Semantic Web Search



Roger Federer

Tennis player



rogerfederer.com

Roger Federer is a Swiss professional tennis player who is currently ranked world No. 10 by the Association of Tennis Professionals. Many players and analysts have called him the greatest tennis player of all time. [Wikipedia](#)

Born: August 8, 1981 (age 35 years), Basel, Switzerland

Height: 1.85 m

Weight: 85 kg

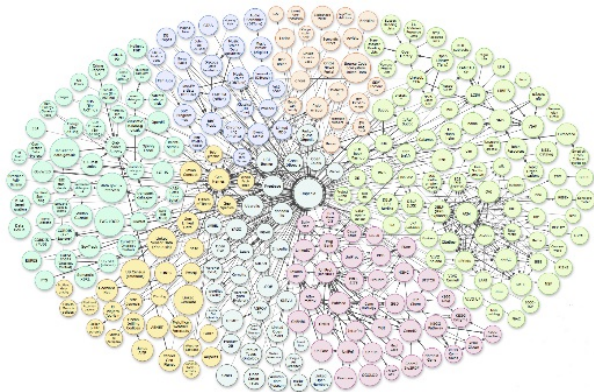
Spouse: [Mirka Federer](#) (m. 2009)

Children: [Lenny Federer](#), [Myla Rose Federer](#), [Charlene Riva Federer](#), [Leo Federer](#)

Semantic Web Search

Google

$\exists X$ winnerOf(X, AustralianOpen2017)



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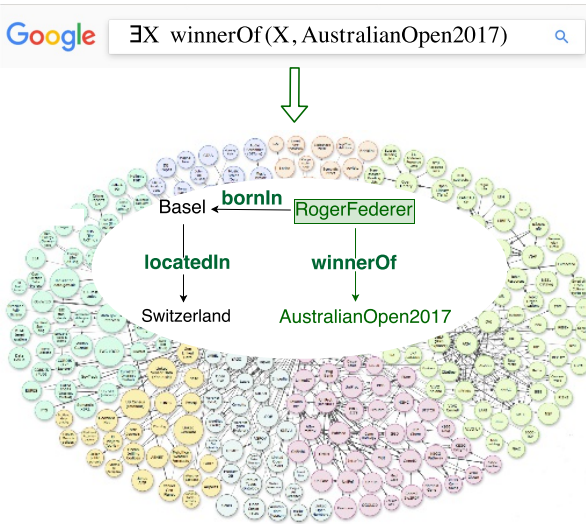
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Knowledge Graphs

← https://en.wikipedia.org/wiki/Roger_Federer 83% Search ☆ 📁 📧 📌 🏠 🔍

"Federer" redirects here. For other uses, see Federer (disambiguation).

Roger Federer (born 8 August 1981) is a Swiss professional tennis player. Many players and analysts have called him the greatest tennis player of all time.^[a] Federer turned professional in 1998 and was continuously ranked in the top 10 from October 2002 to November 2016.^[19] He is currently ranked world No. 4 by the Association of Tennis Professionals (ATP).^[20]


Federer has won 18 Grand Slam singles titles, the most in history for a male tennis player, and held the No. 1 spot in the ATP rankings for a total of 302 weeks. In majors, Federer has won seven Wimbledon titles, five Australian Open titles, five US Open titles and one French Open title. He is among the eight men to capture a career Grand Slam. He has reached a record 28 men's singles Grand Slam finals, including 10 in a row from the 2005 Wimbledon Championships to the 2007 US Open.

Federer's ATP tournament records include winning a record six ATP World Tour Finals and playing in the finals at all nine ATP Masters 1000 tournaments. He also won the Olympic gold medal in doubles with his compatriot Stan Wawrinka at the 2008 Summer Olympic Games and the Olympic silver medal in singles at the 2012 Summer Olympic Games. Representing Switzerland, he was a part of the 2014 winning Davis Cup team. He was named the Laureus World Sportsman of the Year for a record four consecutive years from 2005 to 2008.

Contents (hide)

- 1 Personal life
 - 1.1 Childhood and early life
 - 1.2 Family
 - 1.3 Philanthropy and outreach
- 2 Tennis career
 - 2.1 Pre-1998: Junior years
 - 2.2 1998–2002: Early career and breakthrough in the ATP
 - 2.3 2003: Wimbledon victory
 - 2.4 2004: Imposing dominance
 - 2.5 2005: Consolidating dominance
 - 2.6 2006: Career best season
 - 2.7 2007: Holding off young rivals
 - 2.8 2008: Fifth US Open title, Olympic Gold, and mono
 - 2.9 2009: Career Grand Slam, and major title record
 - 2.10 2010: Fourth Australian Open
 - 2.11 2011: Sixth World Tour Finals title
 - 2.12 2012: Seventh Wimbledon and return to No. 1
 - 2.13 2013: Injury struggles
 - 2.14 2014: Wimbledon runner-up, and Davis Cup win
 - 2.15 2015: 1,000th win, Wimbledon and US Open runners-up
 - 2.16 2016: Knee surgery and long injury break
 - 2.17 2017: Resurgence and 18th major title
- 3 National representation
 - 3.1 Davis Cup
 - 3.2 Olympics
- 4 Rivalries
 - 4.1 Federer vs. Nadal
 - 4.2 Federer vs. Djoković
 - 4.3 Federer vs. Murray
 - 4.4 Federer vs. Roddick
 - 4.5 Federer vs. Hewitt
 - 4.6 Federer vs. Agassi
 - 4.7 Federer vs. del Potro
 - 4.8 Federer vs. Safin

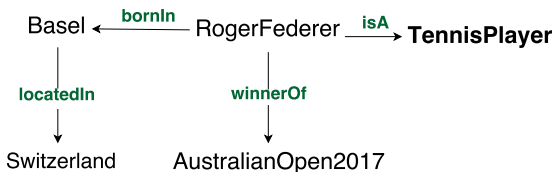
Roger Federer



Federer at 2009 Wimbledon where he broke the Grand Slam record

Country (sports)	 Switzerland
Residence	Böteningen, Switzerland ^[1]
Born	8 August 1981 (age 35) Basel, Switzerland
Height	1.85 m (6 ft 1 in) ^[2]
Turned pro	1998
Plays	Right-handed (one-handed backhand)
Prize money	US\$ 103,990,195
Official website	rogerfederer.com ^g
	Singles
Career record	1099–246 (81.71% in Grand Slam and ATP World Tour main draw matches, in Summer Olympics and in Davis Cup)
Career titles	91 (3rd in the Open Era)
Highest ranking	No. 1 (2 February 2004)
Current ranking	No. 4 (3 April 2017) ^[3]
	Grand Slam Singles results
Australian Open W	(2004, 2006, 2007, 2010, 2017)

Knowledge Graphs

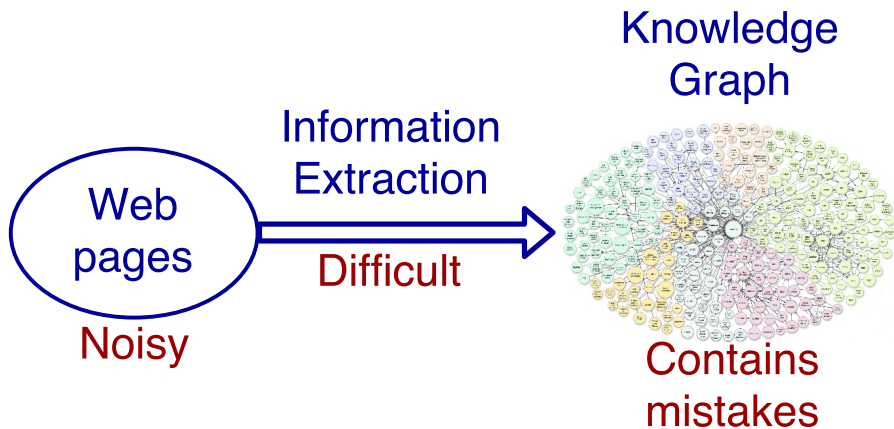


KGs are huge collections of positive unary and binary facts

tennisPlayer(rogerFederer)
bornIn(rogerFederer, basel)

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Problem: Inconsistency



Problem: Incompleteness

Google KG **misses** Roger's living place, but contains his wife's Mirka's..

living place of Roger Federer 🔍

[All](#) [Images](#) [News](#) [Videos](#) [Shopping](#) [More](#) [Settings](#) [Tools](#)

About 2.690.000 results (0,55 seconds)

Roger Federer's glass mansion: Tennis star's £6.5m Swiss waterfront ...
www.telegraph.co.uk › Sport › Tennis › Roger Federer ▼
 Tennis star **Roger Federer** is to move his family into a £6.5million glass mansion on the shores of Lake Zurich after work was completed on the state-of-the-art ...


Roger Federer's Luxurious Houses | Basel Shows
www.baselshows.com/basel-world/the-houses-of-roger-federer ▼
Roger Federer also owns a lavish apartment in Dubai apart from properties in Switzerland. He has chosen this **location** as a base of training to get use to heat ...

living place of Mirka Federer 🔍

[All](#) [Images](#) [News](#) [Shopping](#) [Videos](#) [More](#) [Settings](#) [Tools](#)

About 1.910.000 results (0,92 seconds)

Mirka Federer / Residence



Bottingen, Switzerland

Motivation

Important problems of KGs:

- ① Inconsistency
- ② Incompleteness

In this talk: Reasoning on top of KGs to address these issues

- ① **Deduction**: detecting and **repairing inconsistencies**
- ② **Induction**: learning common-sense rules and **completing** KGs

Overview

✓ Motivation

Ontologies and Rules

Inconsistencies in DL-programs

Nonmonotonic Rule Mining

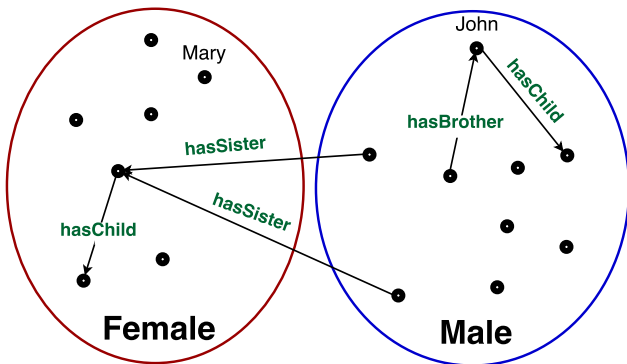
Further and Future Work

History of Knowledge Representation

- **1950's:** First Order Logic (FOL) for KR (**undecidable**)
(e.g. [McCarthy, 1959])
- **1970's:** Network-shaped structures for KR (**no formal semantics**)
(e.g. semantic networks [Robinson, 1965], frames [Minsky, 1985])
- **1979:** Encoding of network-shaped structures into FOL [Hayes, 1979]
- **1980's:** Description Logics (DL) for KR
 - Decidable fragments of FOL
 - Theories encoded in DLs are called **ontologies**
 - Many DLs with different expressiveness and computational features
 - Particularly suited for **conceptual reasoning**

Description Logic Ontologies

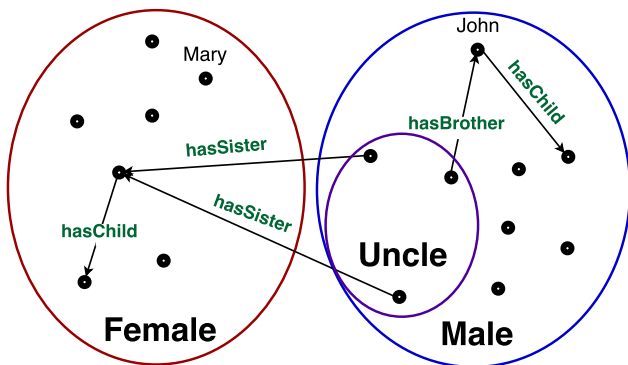
Open World Assumption (OWA): what is not derived is **unknown**



Inclusions: $Female \sqsubseteq \neg Male, hasSister \sqsubseteq hasSibling, hasBrother \sqsubseteq hasSibling$

Description Logic Ontologies

Open World Assumption (OWA): what is not derived is **unknown**



Inclusions: $Female \sqsubseteq \neg Male, hasSister \sqsubseteq hasSibling, hasBrother \sqsubseteq hasSibling$

Complex axioms: $Uncle \equiv Male \sqcap \exists hasSibling. \exists hasChild$

What can not be said in DLs?

- Exceptions from theories (due to **monotonicity**)

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WithBeard \sqsubseteq *Male*

Female \sqsubseteq \neg *Male*

WithBeard(*c*)

People with beards are male

Female are not male

C has a beard

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Male(*c*)

C is male

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- Exceptions from theories (due to **monotonicity**)

WithBeard \sqsubseteq *Male*

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WithBeard(*c*)

Female(*c*)

Male(*c*)

\neg *Male*(*c*)



People with beards are male

Female are not male

C has a beard

C is female

C is male

C is not male

Monotonicity: the more we add, the more we get!

History of Knowledge Representation

- **1970's:** Logic programming
(e.g. Prolog)
- **1980's:** Nonmonotonic logics
(e.g. circumscription [McCarthy, 1980], default logic [Reiter, 1980])
- **1988:** Nonmonotonic rules under answer set semantics (ASP)
[Gelfond and Lifschitz, 1988]
 - Logic programs with model-based semantics
 - Disjunctive datalog with default negation *not*

Not is not \neg !

Default negation *not*

At a rail road crossing cross the road if **no train is known** to approach

walk \leftarrow *at*(*X*), *crossing*(*X*), **not** *train_approaches*(*X*)

Classical negation \neg

At a rail road crossing cross the road if **no train** approaches

walk \leftarrow *at*(*X*), *crossing*(*X*), \neg *train_approaches*(*X*)

Nonmonotonic Rules

Closed World Assumption (CWA): what is not derived is **false**

Rule: $\underbrace{a_1 \vee \dots \vee a_k}_{\text{head}} \leftarrow \underbrace{b_1, \dots, b_m, \text{not } b_{m+1}, \dots, \text{not } b_n}_{\text{body}}$

Informal semantics: If b_1, \dots, b_m are true and **none** of b_{m+1}, \dots, b_n is **known**, then at least one among a_1, \dots, a_k must be true

Default negation: unless a child is adopted one of his parents must be female

$$\text{female}(Y) \vee \text{female}(Z) \leftarrow \text{hasParent}(X, Y), \text{hasParent}(X, Z), \\ Y \neq Z, \text{not adopted}(X)$$

Constraint: ensure that no one is a parent of himself

$$\perp \leftarrow \text{parent}(X, Y), \text{parent}(Y, X)$$

Answer Set Programs

Evaluation of ASP programs is model-based

Answer set program (ASP) is a set of nonmonotonic rules

(1) *hasParent(john, pat)* (2) *hasParent(john, alex)* (3) *male(alex)*
(4) *female(Y) ← hasParent(X, Y), hasParent(X, Z),*
Y ≠ Z, male(Z), not adopted(X)

Answer Set Programs

Evaluation of ASP programs is model-based

1. **Grounding**: substitute all **variables with constants** in all possible ways

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male(alex), not adopted(john)

$I = \{hasParent(john, pat), hasParent(john, alex), male(alex), female(pat)\}$

CWA: *adopted(john)* can not be derived, thus it is false

Answer Set Programs

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(5) *adopted(john)*

adopted(john)

$I = \{ \textit{hasParent(john, pat)}, \textit{hasParent(john, alex)}, \textit{male(alex)}, \textit{female(pat)} \}$

Nonmonotonicity: adding facts might lead to loss of consequences!

Combining Ontologies and Rules

DL Ontologies

Open-World
Assumption

Monotonic

Conceptual reasoning

...

Rules

Closed-World
Assumption

Nonmonotonic

Defaults and exceptions

...

Combining Ontologies and Rules

Hybrid Knowledge Bases

MKNF, DL-safe rules, **DL-programs...**

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Overview

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- ✓ Ontologies and Rules
- Inconsistencies in DL-programs**
- Nonmonotonic Rule Mining
- Further and Future Work



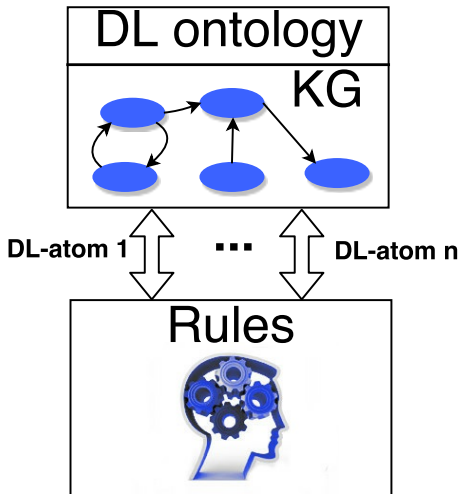
T. Eiter



M. Fink

DL-programs

DL-programs: loose coupling of **ontologies** and **rules** [Eiter *et al.*, 2008]



DL-program

DL ontology

Logical part

- (1) $Child \sqsubseteq \exists hasParent$
- (2) $Female \sqsubseteq \neg Male$
- (3) $Adopted \sqsubseteq Child$

Data part (KG)

- (4) $Male(pat)$
- (5) $Male(john)$
- (6) $hasParent(john, pat)$

Rules

(7) $isChildOf(john, alex)$ (8) $boy(tim)$

(9) $hasFather(john, pat) \leftarrow$  , 

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Answer set: $I = \{isChildOf(john, alex), boy(tim), hasFather(john, pat)\}$

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- (8) $boy(tim)$
- (9) $hasFather(john, pat) \leftarrow DL[; hasParent](john, pat),$
 $DL[Male \uplus boy; Male](pat)$
- (10) $\perp \leftarrow hasFather(john, pat), isChildOf(john, alex),$
 $not DL[; Adopted](john),$
 $not DL[Child \uplus boy; \neg Male](alex)$

Inconsistent DL-program

DL ontology

Logical part

- (1) $Child \sqsubseteq \exists hasParent$
- (2) $Female \sqsubseteq \neg Male$
- (3) $Adopted \sqsubseteq Child$

Data part (KG)

- (4) $Male(pat)$
- (5) $Male(john)$
- (6) $hasParent(john, pat)$

Rules

- (7) $isChildOf(john, alex)$
- (8) $boy(tim)$
- (9) $hasFather(john, pat) \leftarrow DL[; hasParent](john, pat),$
 $DL[Male \uplus boy; Male](pat)$
- (10) $\perp \leftarrow hasFather(john, pat), isChildOf(john, alex),$
 $not DL[; Adopted](john),$
 $not DL[Child \uplus boy; \neg Male](alex)$

Inconsistent DL-program: no answer sets!

DL-program Repair

DL ontology

Logical part

- (1) $Child \sqsubseteq \exists hasParent$
- (2) $Female \sqsubseteq \neg Male$
- (3) $Adopted \sqsubseteq Child$

Data part (KG)

- (4) $Male(pat)$ $Female(alex)$
- (5) $Male(john)$
- (6) $hasParent(john, pat)$

Rules

- (7) $isChildOf(john, alex)$ (8) $boy(tim)$
- (9) $hasFather(john, pat) \leftarrow DL[; hasParent](john, pat),$
 $DL[Male \uplus boy; Male](pat)$
- (10) $\perp \leftarrow hasFather(john, pat), isChildOf(john, alex),$
 $not DL[; Adopted](john),$
 $not DL[Child \uplus boy; \neg Male](alex)$

Repair answer set: $I = \{isChildOf(john, alex), boy(tim), hasFather(john, pat)\}$

DL-program Repair

DL ontology

Logical part

- (1) $Child \sqsubseteq \exists hasParent$
- (2) $Female \sqsubseteq \neg Male$
- (3) $Adopted \sqsubseteq Child$

Data part (KG)

- (4) ~~$Male(pat)$~~ $Female(pat)$
- (5) $Male(john)$
- (6) $hasParent(john, pat)$

Rules

- (7) $isChildOf(john, alex)$ (8) $boy(tim)$
- (9) $hasFather(john, pat) \leftarrow DL[; hasParent](john, pat),$
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- (10) $\perp \leftarrow hasFather(john, pat), isChildOf(john, alex),$
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 $not DL[Child \uplus boy; \neg Male](alex)$

Repair answer set: $I = \{isChildOf(john, alex), boy(tim)\}$

DL-program Repair

DL ontology

Logical part

- (1) $Child \sqsubseteq \exists hasParent$
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Rules

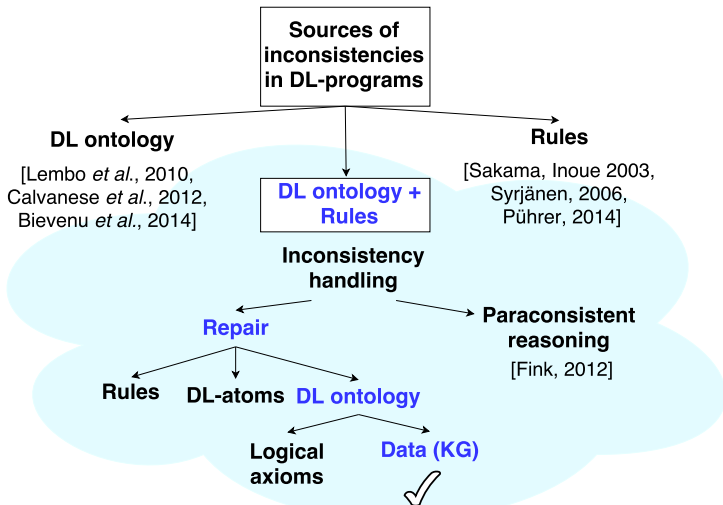
- (7) $isChildOf(john, alex)$ (8) $boy(tim)$
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- (10) $\perp \leftarrow hasFather(john, pat), isChildOf(john, alex),$
 $not DL[; Adopted](john),$
 $not DL[Child \uplus boy; \neg Male](alex)$

Repair answer set: $I = \{isChildOf(john, alex), boy(tim)\}$

Inconsistency Handling in DL-programs

Goal: develop techniques for handling inconsistencies in DL-programs

Approach: repair ontology data part (KG) to regain consistency



Complexity of Repair Answer Sets

INSTANCE: A ground DL-program $\Pi = \langle O, P \rangle$.

QUESTION: Does there exist a repair answer set for Π ?

Theorem

Deciding repair and standard answer set existence have the same complexity if instance query-answering in O is polynomial ($DL\text{-Lite}_{\mathcal{A}}, \mathcal{EL}$).

Π	FLP semantics	weak semantics
normal	Σ_2^P -complete	NP-complete
disjunctive	Σ_2^P -complete	Σ_2^P -complete

Ontology Repair Problem

INSTANCE: Ontology O , $D_{true} = \{\langle update, query \rangle\}$, $D_{false} = \{\langle update, query \rangle\}$

QUESTION: Does there exist O data part, for which queries under their updates from D_{true} are true and from D_{false} are false?

Theorem

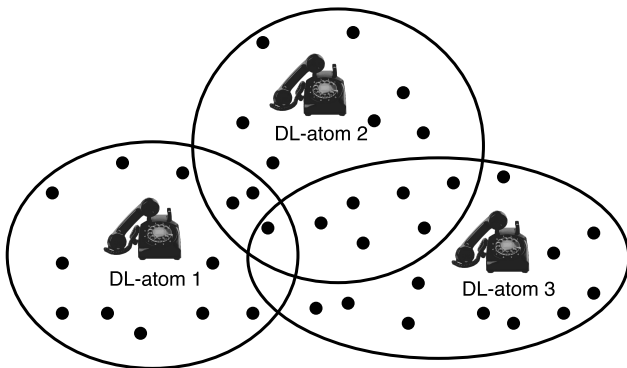
The Ontology Repair Problem is NP-complete even if $O = \emptyset$.

Tractable cases:

- Deletion repair
- Bounded addition
- Bounded change
- ...

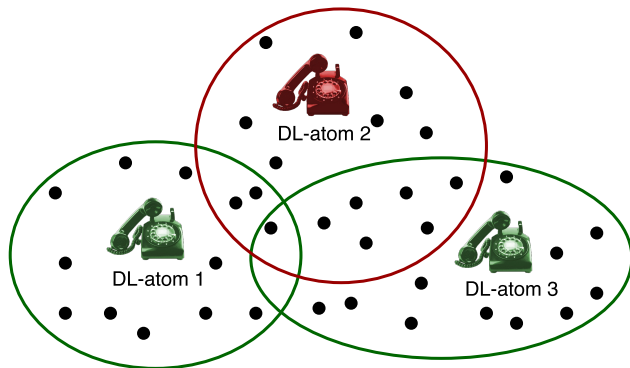
Optimized DL-program Repair

- For each DL-atom compute minimal sets of facts (●), whose presence in ontology ensures DL-atom's query entailment (small for some DLs)



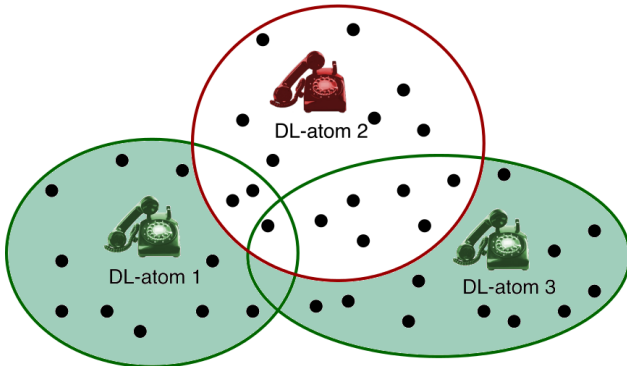
Optimized DL-program Repair

- For each DL-atom compute **minimal sets of facts** (●), whose presence in ontology **ensures DL-atom's query entailment** (small for some DLs)
- **Guess values of DL-atoms** under which the program has an answer set



Optimized DL-program Repair

- For each DL-atom compute **minimal sets of facts** (●), whose presence in ontology **ensures DL-atom's query entailment** (small for some DLs)
- **Guess values of DL-atoms** under which the program has an answer set
- Solve **ontology repair problem** as a variant of a **hitting set problem**



Example Benchmark



- **Ontology:** MyITS¹
 - **personalized route planning** with semantic information
 - logical axioms (406), (building features located inside private areas are not publicly accessible, covered bus stops are those with roofs)
 - KG (4195 facts), Cork city map with leisure areas, bus stops,...
- **Rules:** check that public stations don't lack public access, using CWA on private areas
- **Inconsistency:** wrong GPS coordinates result in roofed bus stops being located inside private areas
- **Repair:** found within 12 seconds

¹ <http://www.kr.tuwien.ac.at/research/projects/myits/>

Overview

- ✓ Motivation
- ✓ Ontologies and Rules
- ✓ Inconsistencies in DL-programs

Nonmonotonic Rule Mining



M. Gad-Elrab



J. Urbani



G. Weikum



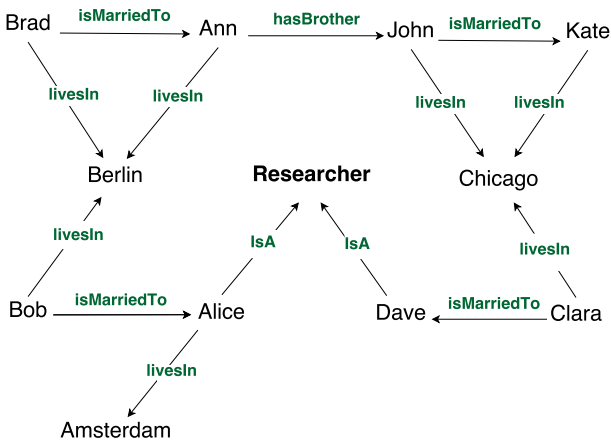
D. H. Tran



F. A. Lisi

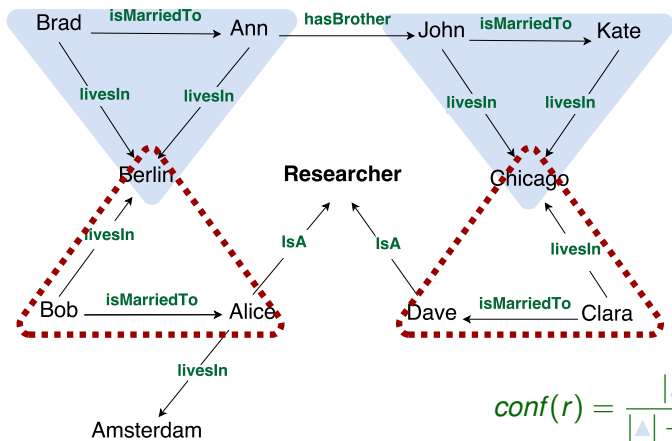
Further and Future Work

Horn Rule Mining



Horn Rule Mining

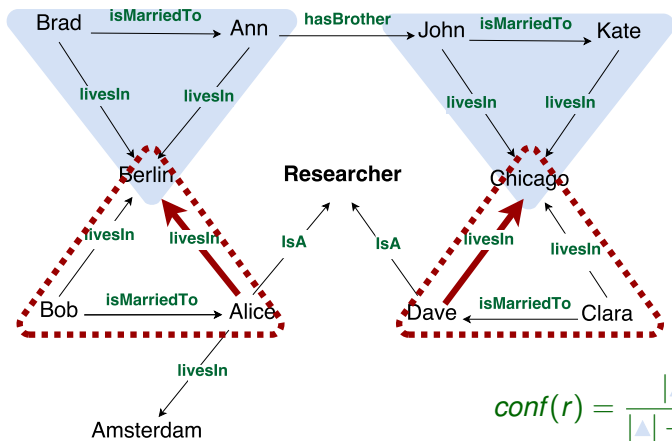
Horn rule mining for KG completion [Galárraga *et al.*, 2015]



$r : livesIn(X, Z) \leftarrow isMarriedTo(Y, X), livesIn(Y, Z)$

Horn Rule Mining

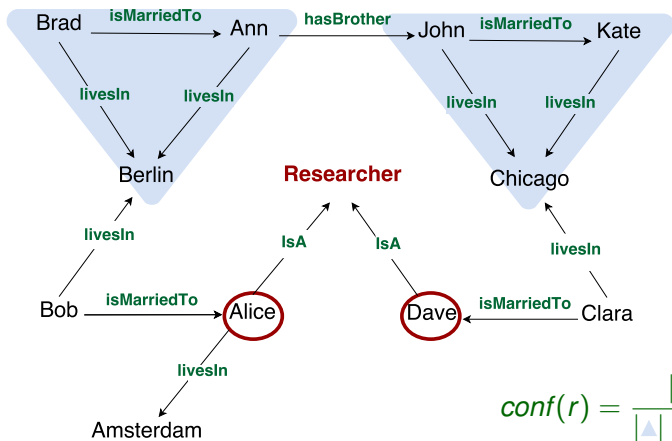
Horn rule mining for KG completion [Galárraga *et al.*, 2015]



$r : livesIn(X, Z) \leftarrow isMarriedTo(Y, X), livesIn(Y, Z)$

Nonmonotonic Rule Mining

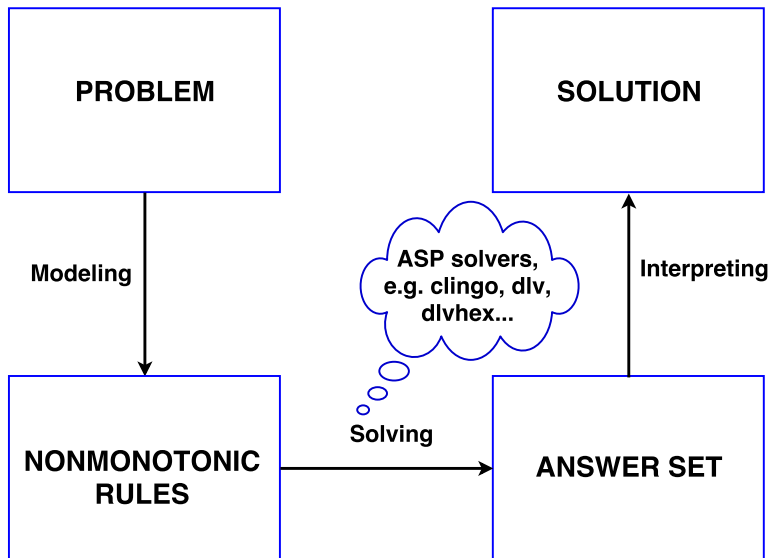
Nonmonotonic rule mining from KGs: **OWA** is a challenge!



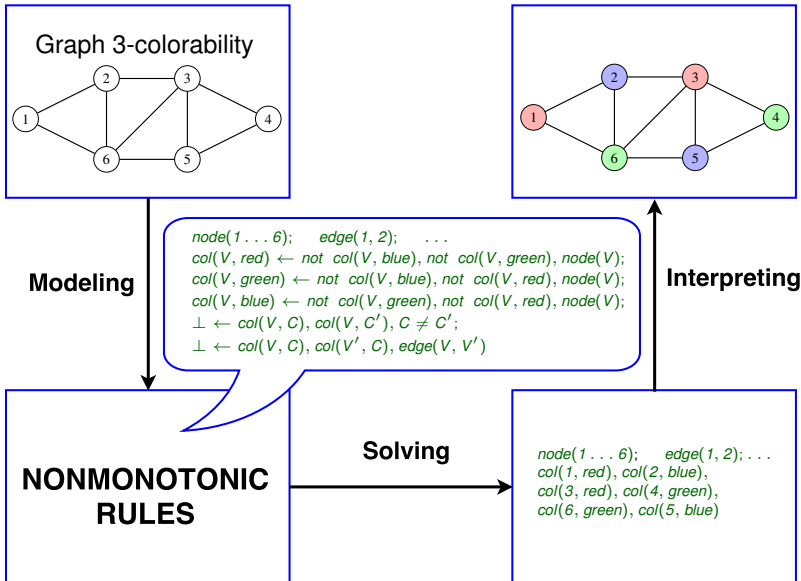
$$conf(r) = \frac{|\triangle|}{|\triangle| + |\triangle|} = 1$$

$r : livesIn(X, Z) \leftarrow isMarriedTo(Y, X), livesIn(Y, Z), not\ researcher(X)$

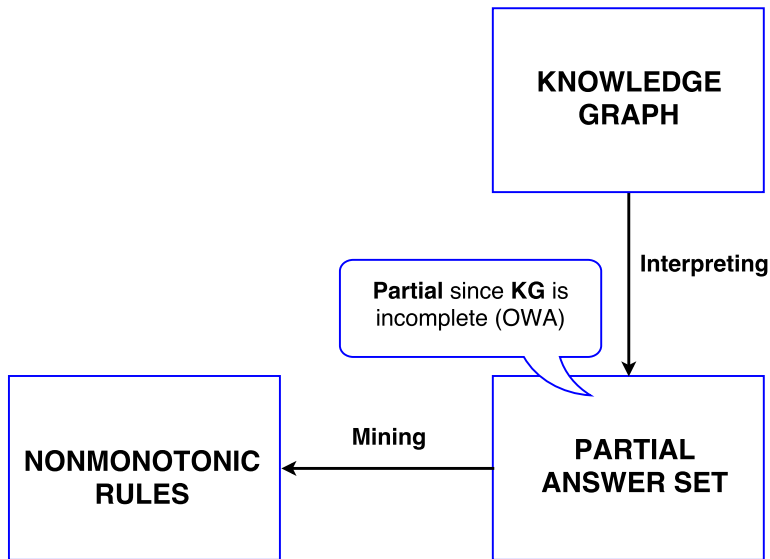
Declarative Programming Paradigm



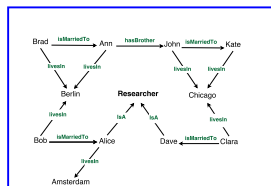
Declarative Programming Example



Nonmonotonic Rule Mining



Nonmonotonic Rule Mining



Interpreting

```

    isMarriedTo(brad, ann);
    isMarriedTo(john, kate);
    isMarriedTo(bob, alice);
    isMarriedTo(clara, dave);
    livesIn(brad, berlin);
    . . .
    researcher(alice);
    researcher(dave)
  
```

Mining

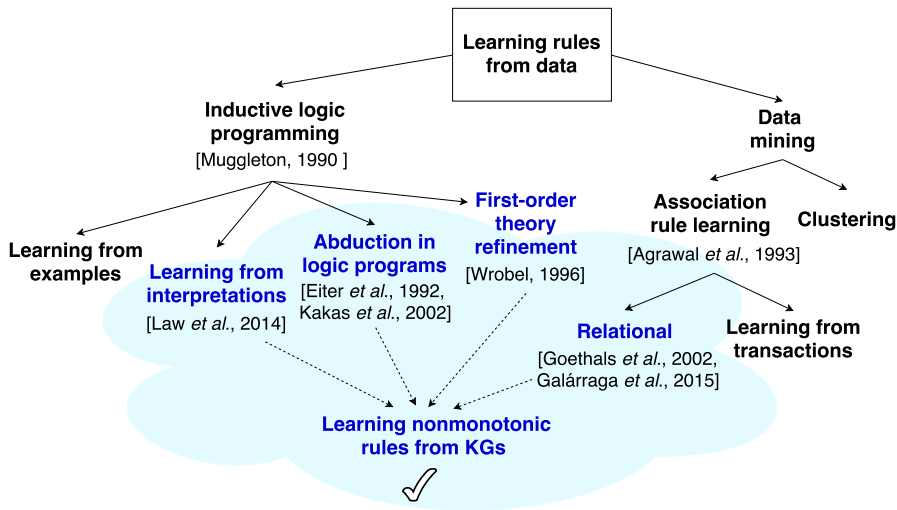
```

    livesIn(Y, Z) ← isMarried(X, Y),
                   livesIn(X, Y),
                   not researcher(Y)
  
```

Nonmonotonic Rule Mining from KGs

Goal: learn nonmonotonic rules from KG

Approach: revise association rules learned using data mining methods

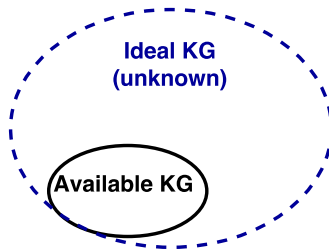


Horn Theory Revision

Quality-based Horn Theory Revision

Given:

- Available KG

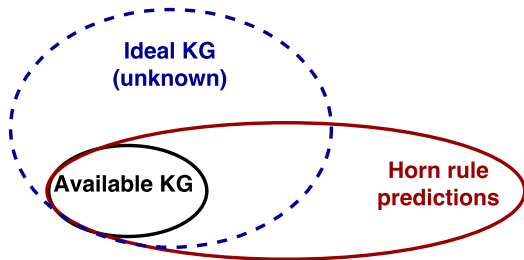


Horn Theory Revision

Quality-based Horn Theory Revision

Given:

- Available KG
- Horn rule set

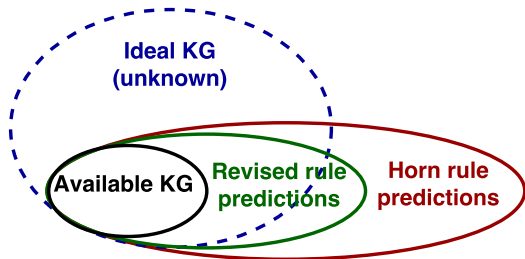


Horn Theory Revision

Quality-based Horn Theory Revision

Given:

- Available KG
- Horn rule set



Find:

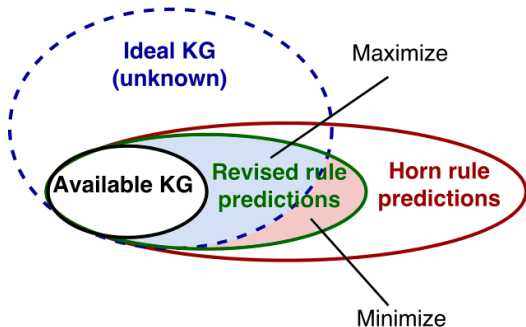
- Nonmonotonic revision of Horn rule set

Horn Theory Revision

Quality-based Horn Theory Revision

Given:

- Available KG
- Horn rule set



Find:

- Nonmonotonic revision of Horn rule set with better predictive quality

Avoid Data Overfitting

How to distinguish exceptions from noise?

$r1 : \text{livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{not } \text{researcher}(X)$

Avoid Data Overfitting

How to distinguish exceptions from noise?

$r1 : \text{livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{not } \text{researcher}(X)$
 $\text{not_livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{researcher}(X)$

Avoid Data Overfitting

How to distinguish exceptions from noise?

$r1 : \text{livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{not researcher}(X)$
 $\text{not_livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{researcher}(X)$

$r2 : \text{livesIn}(X, Z) \leftarrow \text{bornIn}(X, Z), \text{not moved}(X)$
 $\text{not_livesIn}(X, Z) \leftarrow \text{bornIn}(X, Z), \text{moved}(X)$

Avoid Data Overfitting

How to distinguish exceptions from noise?

$r1 : \text{livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{not researcher}(X)$
 $\text{not_livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z), \text{researcher}(X)$

$r2 : \text{livesIn}(X, Z) \leftarrow \text{bornIn}(X, Z), \text{not moved}(X)$
 $\text{not_livesIn}(X, Z) \leftarrow \text{bornIn}(X, Z), \text{moved}(X)$

$\{\text{livesIn}(c, d), \text{not_livesIn}(c, d)\}$ are conflicting predictions

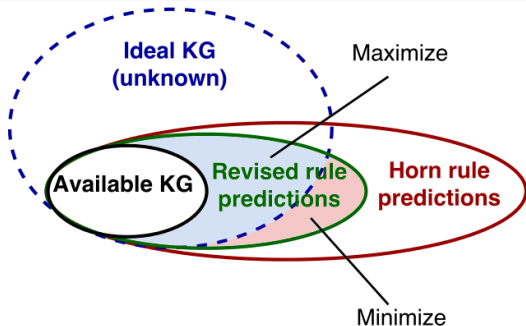
Intuition: Rules with good exceptions should make few conflicting predictions

Horn Theory Revision

Quality-based Horn Theory Revision

Given:

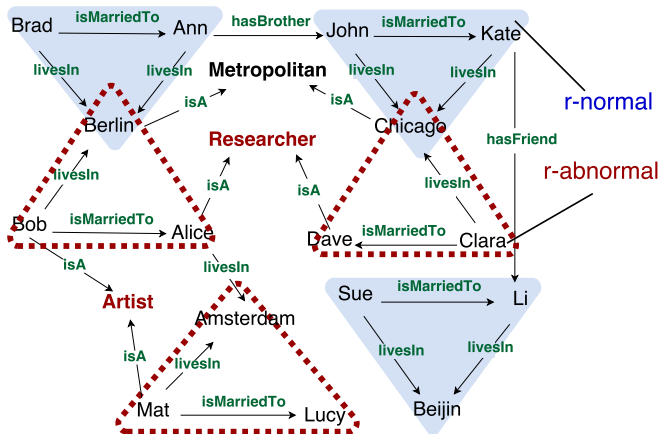
- Available KG
- Horn rule set



Find:

- Nonmonotonic revision of Horn rules, such that
 - number of **conflicting predictions** is **minimal**
 - average **conviction** is **maximal**

Exception Candidates



$r: \text{livesIn}(X, Z) \leftarrow \text{isMarriedTo}(Y, X), \text{livesIn}(Y, Z)$

$\left\{ \begin{array}{l} \text{not researcher}(X) \\ \text{not artist}(Y) \end{array} \right\}$

Exception Ranking

rule1 $\{\underline{e}_1, e_2, e_3, \dots\}$

rule2 $\{e_1, \underline{e}_2, e_3, \dots\}$

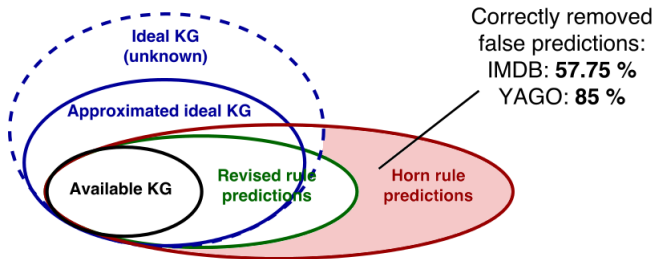
rule3 $\{\underline{e}_1, e_2, e_3, \dots\}$

Finding globally best revision is expensive, exponentially many candidates!

- **Naive ranking:** for every rule inject exception that results in the highest conviction
- **Partial materialization (PM):** apply all rules apart from a given one, inject exception that results in the highest average conviction of the rule and its rewriting
- **Ordered PM (OPM):** same as PM plus ordered rules application
- **Weighted OPM:** same as OPM plus weights on predictions

Experimental Setup

- **Approximated ideal KG**: original KG
- **Available KG**: for every relation randomly remove 20% of facts from approximated ideal KG
- **Horn rules**: $h(X, Y) \leftarrow p(X, Z), q(Z, Y)$
- **Exceptions**: $e_1(X), e_2(Y), e_3(X, Y)$
- **Predictions** are computed using **answer set solver** DLV



Experimental Setup

- **Approximated ideal KG**: original KG
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- **Exceptions**: $e_1(X), e_2(Y), e_3(X, Y)$
- **Predictions** are computed using **answer set solver** DLV

Examples of revised rules:

Plots of films in a sequel are written by the same writer, unless a film is American

$r_1 : \text{writtenBy}(X, Z) \leftarrow \text{hasPredecessor}(X, Y), \text{writtenBy}(Y, Z), \text{not american_film}(X)$

Spouses of film directors appear on the cast, unless they are silent film actors

$r_2 : \text{actedIn}(X, Z) \leftarrow \text{isMarriedTo}(X, Y), \text{directed}(Y, Z), \text{not silent_film_actor}(X)$

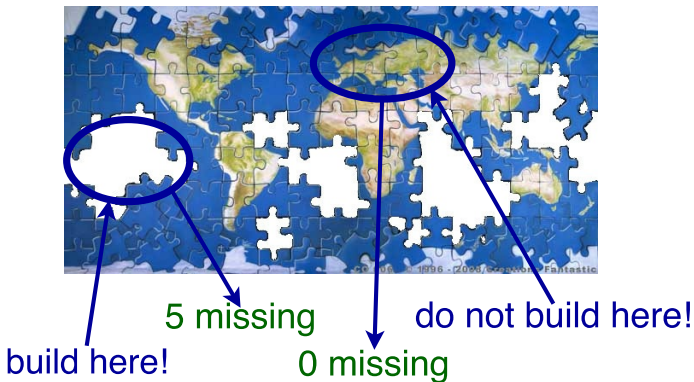
Overview

- ✓ Motivation
- ✓ Ontologies and Rules
- ✓ Inconsistencies in DL-programs
- ✓ Nonmonotonic Rule Mining

Ongoing and Future Work

Completeness-aware Rule Mining

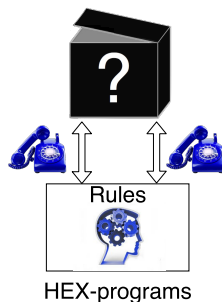
- Exploit **cardinality meta-data** [Mirza *et al.*, 2016] in rule mining
John has 5 children, Mary is a citizen of 2 countries



Ongoing and Future Work

- Make use of **logical background knowledge** in
 - **Rule learning** and other **data mining** tasks²
 - **Information extraction** from text corpora³
 - **Natural language processing** tasks

- Exploit **answer set programs with external computations** [Eiter *et al.*, 2009] for the above problems



² S. Paramonov, D. Stepanova, P. Miettinen. Hybrid Approach to Constraint-based Pattern Mining. Accepted to *RR2017*

³ Joint work with M. Gad-Elrab, J. Urbani, G. Weikum

Conclusion


Summary:


- Inconsistencies in combination of rules and ontologies
 - Repair semantics and its complexity analysis
 - Optimized algorithms for repair computation and their evaluation ($DL-Lite_{\mathcal{A}}$ and \mathcal{EL} DLs)
- Nonmonotonic rule mining from KGs
 - Quality-based Horn theory revision framework under OWA
 - Approach for computing and ranking exceptions based on cross-talk among rules and its evaluation on real-world KGs


Future Directions:


- Interlinking mining and reasoning in the KG context
- Exploiting logical background knowledge in information extraction and natural language processing tasks

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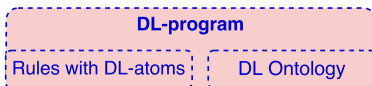
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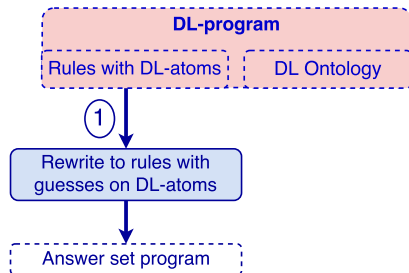
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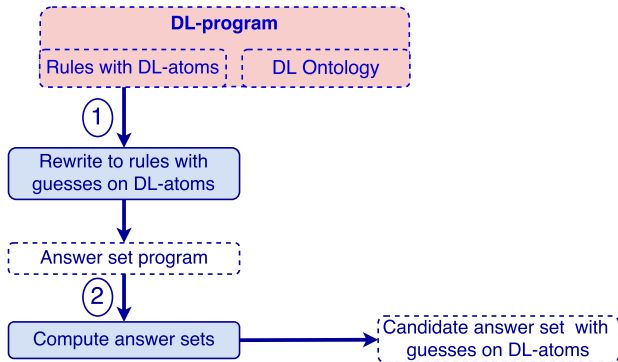
DL-program Repair Algorithm



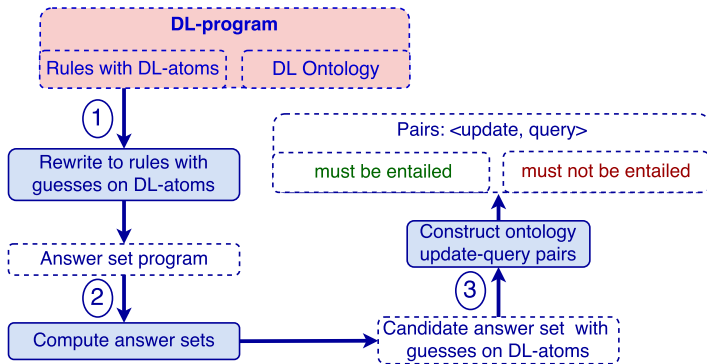
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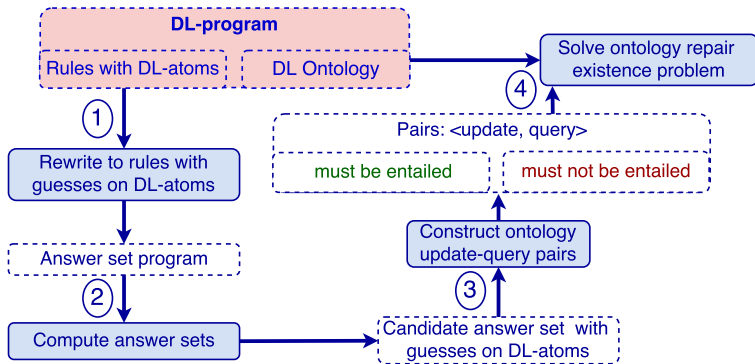
DL-program Repair Algorithm



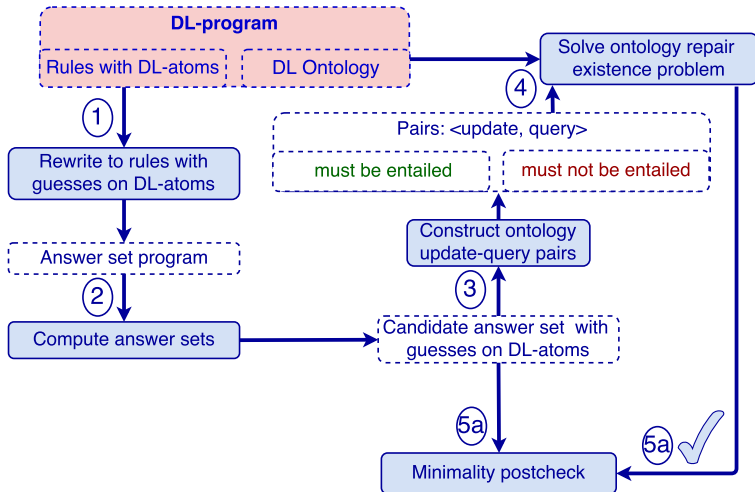
DL-program Repair Algorithm



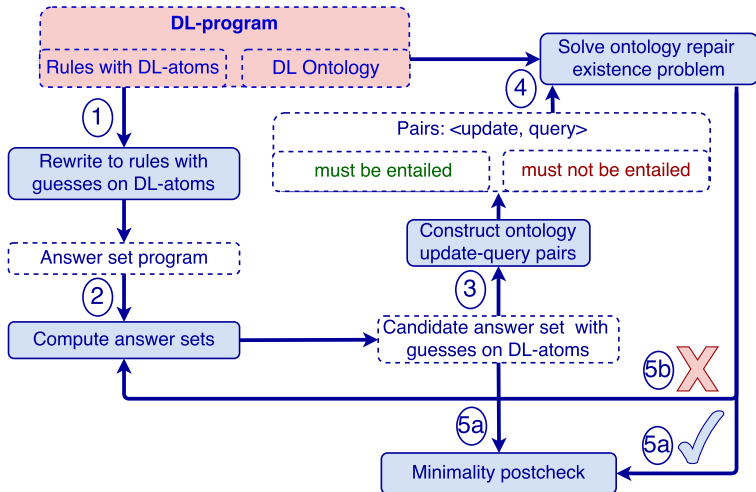
DL-program Repair Algorithm



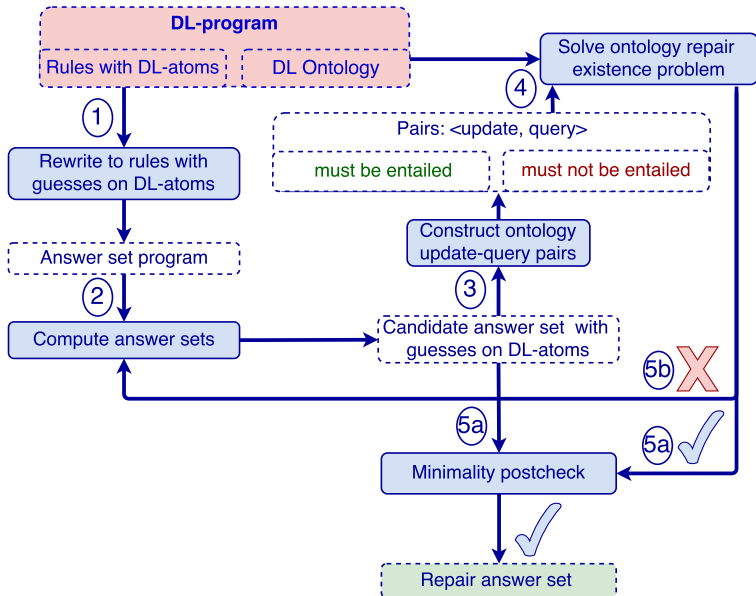
DL-program Repair Algorithm



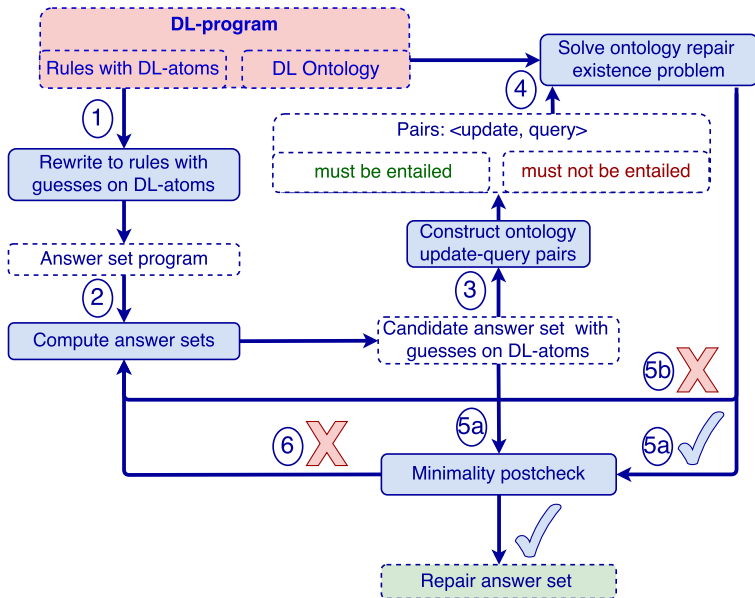
DL-program Repair Algorithm



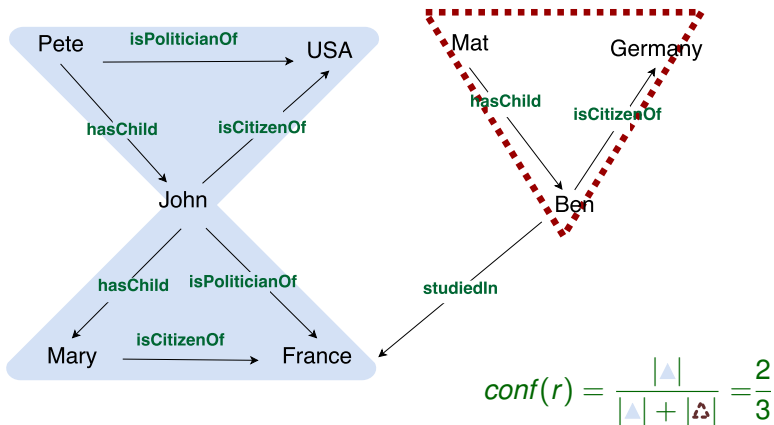
DL-program Repair Algorithm



DL-program Repair Algorithm



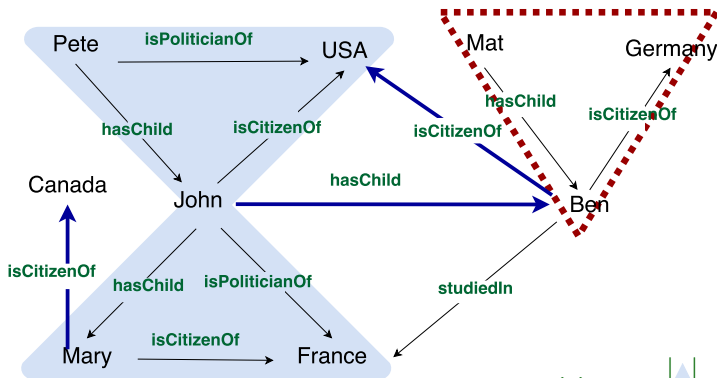
Spurious Rules due to Incompleteness



$r : isPoliticianOf(X, Z) \leftarrow hasChild(X, Y), isCitizenOf(Y, Z)$

Spurious Rules due to Incompleteness

In real world:

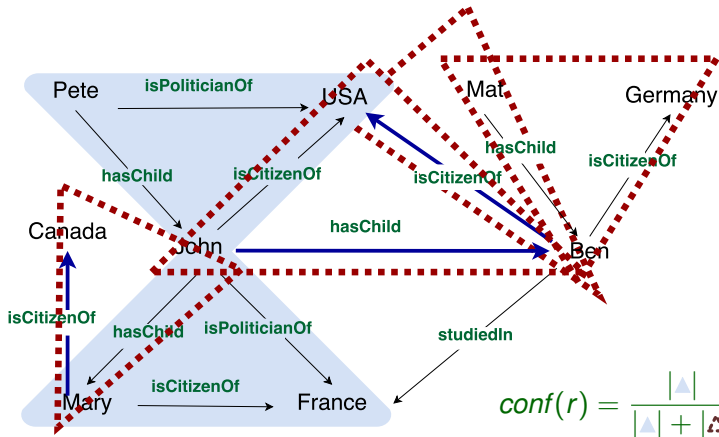


$$conf(r) = \frac{|\triangle|}{|\triangle| + |\triangle|} = \frac{2}{3}$$

$r : isPoliticianOf(X, Z) \leftarrow hasChild(X, Y), isCitizenOf(Y, Z)$

Spurious Rules due to Incompleteness

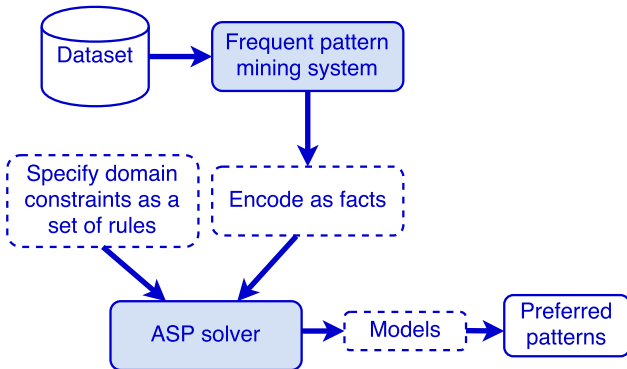
In real world:



$$r : \underbrace{isPoliticianOf(X, Z)}_{complete} \leftarrow \underbrace{hasChild(X, Y), isCitizenOf(Y, Z)}_{incomplete}$$

Hybrid Constraint-based Pattern Mining

- Interlink **mining** and **reasoning**
- Use declarative **logic programming** for frequent pattern (itemset/sequence) filtering
- Combine various **domain-specific** constraints



Semantically-enhanced Fact Spotting

KG population problem: some facts are hard to spot in text due to reporting bias *lost(nadal, australianOpen2017)*

Given:

- Fact: *lost(nadal, australianOpen2017)*
- Rule set: $lost(Z, Y) \leftarrow won(X, Y), finalist(Z, Y), X \neq Z$
- KG: *won(federer, australianOpen2017)*
- Text: "... another **finalist of Australian Open in 2017 was Nadal**"

Find:

- Fact's truth value: *lost(nadal, australianOpen2017)* is true!